

$$u + \frac{1}{u} = u \cdot \frac{1}{u} = 1$$

$$5) \quad u + v = uv = vu = v + u.$$

$$6) \quad u \in \mathbb{R}^+$$

$$\alpha \in \mathbb{R}$$

$$\alpha u = u^\alpha \in \mathbb{R}^+$$

$$7) \quad \alpha(u+v) = \alpha(uv) = (uv)^\alpha = u^\alpha v^\alpha$$

$$\alpha u + \alpha v = u^\alpha + v^\alpha = u^\alpha v^\alpha$$

$$8) \quad (\alpha + \beta)u = (\alpha + \beta)u^{\alpha + \beta} = u^{\alpha + \beta} = u^\alpha \cdot u^\beta = u^\alpha \cdot u^\beta = \alpha u \cdot \beta u = \alpha u + \beta u$$

$$9) \quad \alpha(\beta u) = \alpha(u^\beta) = u^{\alpha\beta}$$

$$(\alpha\beta)u = u^{\alpha\beta}$$

$$\beta(\alpha u) = \beta(u^\alpha) = u^{\alpha\beta}$$

$$10) \quad 1 \cdot u = u^1 = u$$

$\therefore \mathbb{R}^+(\mathbb{R})$ is a vector space.

Ex-6:- $\mathbb{R}^2(\mathbb{R})$

$$\alpha u = \alpha(x, y) = (2\alpha x, \alpha y) \text{ \& normal addition}$$

$\therefore \mathbb{R}^2(\mathbb{R})$ is an abelian group under addition

$$\text{but } 1 \cdot u = 1(x, y) = (2x, y) \neq u$$

$\therefore \mathbb{R}^2(\mathbb{R})$ is not a V.S.